

Level of Measurement

Nominal Categorical Data; names, labels, listings; order is not important

Ordinal Categorical Data; can be arranged in order, but differences between values cannot be found or have no meaning; Ranking; Ex: Low, Medium, High.

Interval Quantitative Data (#); can be arranged by order, differences are meaningful; No natural zero or starting point.

Ratio Highest Level of Quantitative Data; can be arranged in order, differences & division make sense, a starting zero.

- Quiz
- ① Ages (in years) of students = Ratio
 - ② IQs of Students = Interval
 - ③ Ranking of Students Efforts (Good, Better, Best) = Ordinal

Statistics

Statistics Data

- found almost anywhere
- no statistical bias

Definition: Collection, Organization, analysis, interpretation of numerical information.

- Collection = Samples, Experiments, census, simulations \rightarrow (SECS)

Quiz

- ① observational studies
- ② Surveys
- ③ experiments
- ④ anecdotes

stat
↓
Sorc A
↓
L1

randInt \rightarrow can

have same #

TI-84 Calculator

① MATH \rightarrow Prob \rightarrow B1

② lower & upper

③ n \rightarrow Sample Size

④ stat \rightarrow List x

08-21-2023

STATS IS ...

Survey observation	1. Collecting <ul style="list-style-type: none">sampleexperimentcensussimulation	2. Organize
	3. Analysis	4. Interpret

Organize = graph, chart, Table.

Analysis: center / shape / spread / Outliers, Gaps

Trends

Measures of central tendency

of dispersion / spread

Confidence intervals

Hypothesis test

Interpretation: Assumption

P-value & Alpha level
(confidence level)

Z score or Tscore or chi sq score

written summary

Population: Measurements of Entire group of interest

$N = \chi \leftarrow$ population size

{ Data from ALL

Population = kind w/ people

Quantitative variable from ALL

+ Data from all

Categorical variable from ALL

Sample: part of the population

{ Smaller section of those being measured $n = \chi \rightarrow$ Sample size

Data from

the variable of

Random # Sheet

1.1 # 8 a) mpg = variable

① # each car.

b) Quantitative

② Drop an object.

c) Average mile per gallon for all new hybrid small car

③ go up/right/left/down

④ ⚪ number as one, within 001 ~ 550

Random Sample

overcover \rightarrow cover, but too much

⑤ to inspect the car

↓
from
compt list

Undercover \rightarrow Didn't cover.

Google sheet

① number each locker

④ right down corner

② Open google sheet

③ = Rand.Between (1, 1500)

\rightarrow other side

08-23-2023

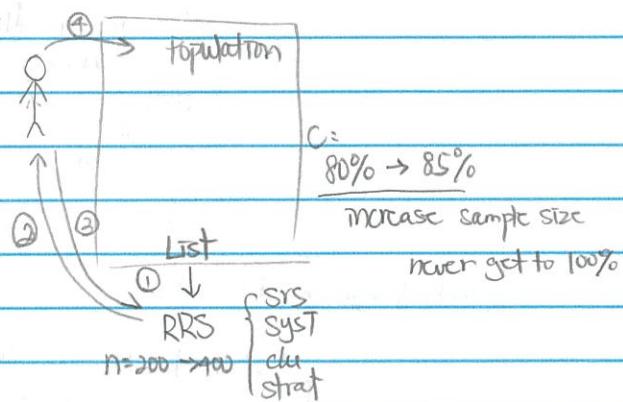
Ch 8 PdF (before Test, probably not now)

Sampling	Simple random ①	Overcover vs. Undercover
	Convenience (X) ②	
	Systematic ③	STATS TS:
	Cluster ④	① Collecting
	Stratified ⑤	② Organize
	① number & random choose	③ Analysis
	② People nearby	④ Interpret
	③ Start point, choose after 0 x x x 0 x x x ...	
	④ cluster (usually by location) (all of the sample in the cluster)	█ █ █ █
	⑤ ↑ then random choose	

Fight Bias!

Inferential Statistic Pic

- To begin well, get a LIST
- Simple Random Sample (SRS)
- Stratified Sample
- Cluster Sample
- Systematic Sample



EX a) Stratified

1.2 (20) b) Simple random (SRS)

Bias = Read PPT

c) Cluster

• Non-Res

d) Systematic

e) Convenience

$$\boxed{n=1,200}$$

each 298

Patient with
chest pain

TI-84 = Random Int No Rep (1, 298, 199)

left over

→ pre-test → Treatment → 3 months.

↓

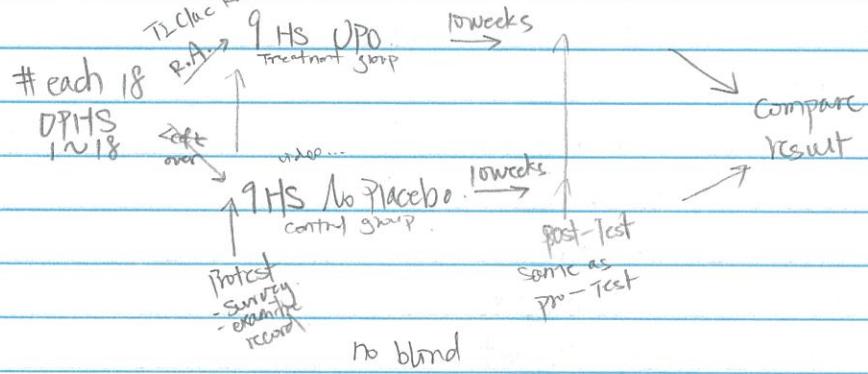
post-test

↓

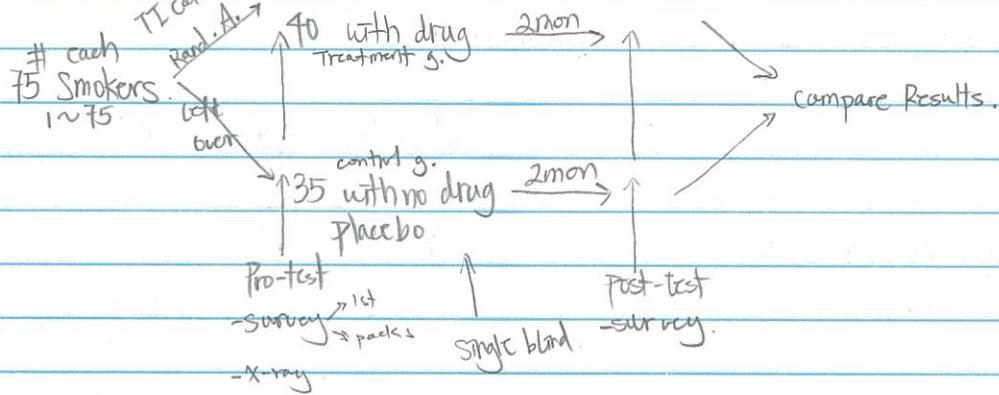
Compare

1.3 (7/10)

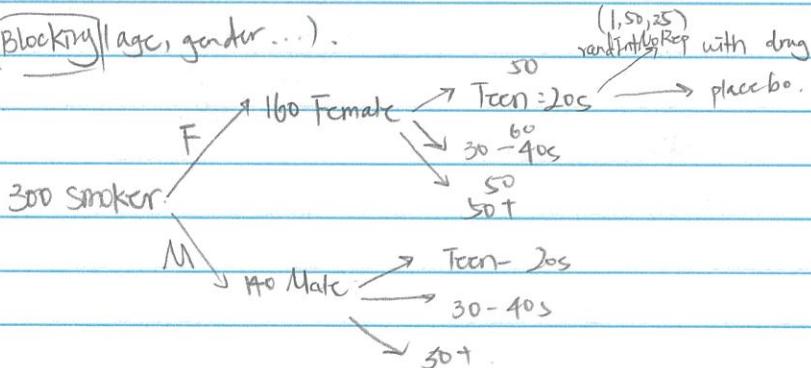
9(b) UPO.
T1 Calc Rand Int No Rep (1,18,1).



9(c) T1 Calc Rand Int No Rep (1,15,4)



(Blocking) age, gender



Simulation

start with model, in some fashion, experiment, a procedure for imitating (simulation), repetition. [TI-84, Computer, RNT]

The imitation of chance behavior, based on a model that accurately reflects the experiment under consideration, is called a simulation

Simulation \star ① State the Prob.

② Assumptions

③ Assign digits, (similar to real outcome)

④ Many Reps. 25^+ time

⑤ State Cond. Sim \approx reality

Example = flip coins

(follow \star)

① Find Hot Streak Coins ($3+3$ same in roll)

② Head \approx Tail equally likely. (50% - 50%) (Toss are Indep.)

③ 0, 1, 2 ... 9, RNT $1/10$ (Indep.) (1 digit = 1 coin) (odd = H, Even = T)

$10 \# = 10$ coin flap = 1 Rep

10 #s

④ Repeat many time (25^+)

⑤ state Cond. \approx

5.56 ① 10 University student about Evening exam

(23-59)

② Assumptions: $\bar{x}/N = 80\% / 20\%$ (student are alone).

- 5.57 ① Simulation of free throws in real High School Basketball game rival/close B.C.P
 ② Assumptions (Indep. shots) (15 feet & 10feet) (no fan's sound) (no wind) (no def.)
 (70%) (not injured).

③ Assigned digit 0,1,2,3,4,5,6 = \$
 7,8,9 = Bluk

Rep¹
 96746 (No)
 Rep²
 12149 (No)
 Rep³
 37823 (No)
 Rep⁴
 71868 (Yes)

X / 25

④ Rep. X / 25. 5 / 25 = 20%

⑤ State cond.

- 6.16 ① Simulate baseball hit major lead 20 at bats.

- 5.60 ② Indep. Pitcher = Reg. x colo Relics. Late Season
 ③ 0,1,2 = Hit (x)(30% ≠ 32%) 00 ~ 31 = Hit, 32 ~ 9 = not hit

Statistic History 08-11-2023

① In the beginning, statistics involved summarizing data by means of charts and table.

② what did the Chinese use statistics for? when?

- Chinese who used statistics for keeping state record. The Chinese under the Chou Dynasty, 2000 B.C., maintained extensive lists of revenue collection and government expenditures, availability of warriors.

③ who began the study of statistics?

Bills of Mortality - The study of statistics was begun by John Graunt. (English) (1620~74)

④ why wasn't statistical theory commonly use prior to 1930? what changed?

- Time consuming, Computer Involved

⑤ what is inference?

- Generalizing on samples.

⑥ Where are the origins of the study of probability found?

- Pascal, Fermat,

⑦ who wrote the first book on the theory of randomness? What was the title?

- Cardan, Italian (1501~1576) The Book On Games of chance



how to live with stats. 2 weeks.

Graph = Information more quickly, efficiently, attractively.

Title! name!

7 second, keep it simple

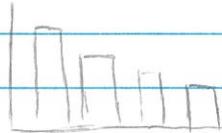
Analysis, trends, why?

Bar Graph: Show Differences

comparing several

Squiggle ↗

Pareto charts = vertical bar graph arranged tall to small



Ojrc

Circle (Pie) graph. ⊖

- % of a whole.

- inside (#) or a key.

Line graph ↗

Picto graph = full symbol

Analysis

- Note the high & low

- Trend

- conjecture, why

1. Misleading.

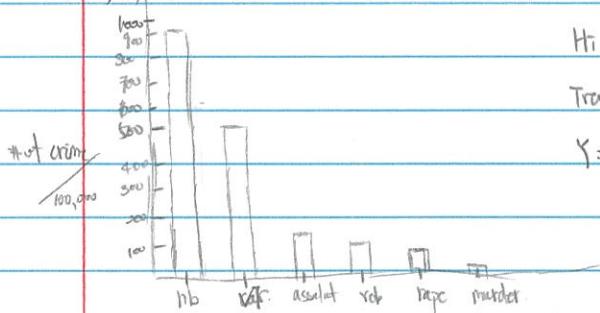
11) a) Hawaiian crime rate

ANA:

Hi, Low house burglary, murder.

Trend = 難度 程度 less violence, more frequent.

Y = easier target for HB & V.I.
usually not super violent.

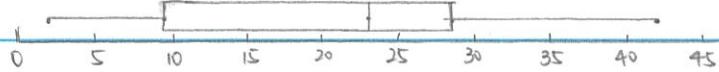


crime tap

10-30-2022

3.3 (7, 8, 11) + Billionaires

$$7. \text{ min} = 2 \quad Q_1 = 9.5 \quad \text{Med} = 23 \quad Q_3 = 28.5 \quad \text{max} = 42$$



center = 23 (Med)

Spread = IQR, 19

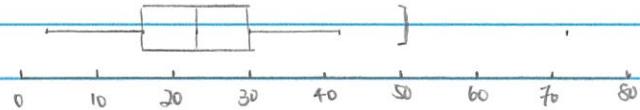
shape = Uniform

$$\text{Outlier} = Q_1 - 1.5 \times \text{IQR} = -26.5$$

$$Q_3 + 1.5 \times \text{IQR} = 57$$

None

$$8. \text{ min} = 3 \quad Q_1 = 16 \quad \text{Med} = 23 \quad Q_3 = 30 \quad \text{max} = 72$$



center = 23 (Med)

Spread = IQR, 14

shape = Uniform

$$\text{Outlier} = Q_1 - 1.5 \times \text{IQR} = -18$$

$$Q_3 + 1.5 \times \text{IQR} = 51$$

72

11) a) lowest = CA , Highest = PA

b) PA

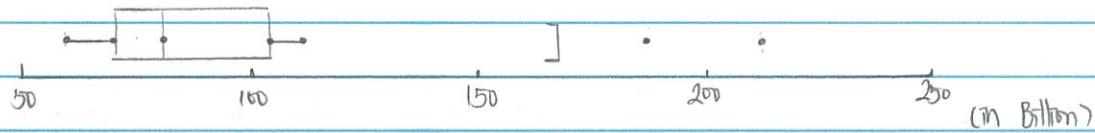
c) CA has smallest range , TX has the smallest interquartile range.

d) CA - (c)

PA - (b)

TX - (a)

Billionaires	① 211	⑪ 80.5	(in Billm)
	② 180	⑫ 79.2	
	③ 114	⑬ 77.3	$\text{Min} = 57.6$
	④ 107	⑭ 76	$Q_1 = 66.2$
	⑤ 106	⑮ 68	$\text{Med} = 80.6$
	⑥ 104	⑯ 64.4	$Q_3 = 105$
	⑦ 94.5	⑰ 59	$\text{Max} = 211$
	⑧ 93	⑱ 59	
	⑨ 83.4	⑲ 58.8	
	⑩ 80.7	⑳ 57.6	



center = 80.6 (Med)

spread = IQR = 38.8 = "small"

shape = skewed right

outlier = $Q_3 + 1.5 \times \text{IQR} = 8$

$Q_3 + 1.5 \times \text{IQR} = 163.2$

180, 211

Unit 5 (ch 4) Probability

- Probability: A measure of chance, likelihood of an event happening
- Probability Notation: $P(A)$ (Prob of event "A")
- Prob Found: f/n ($\# \text{ of desired} / \# \text{ of total result}$)
- Fraction (reduced), Decimal, % s = all good

$$0 \leq P \leq 1$$

$$P(E) = 0.8, 0.9, 0.95$$

contemplate certain $P(c) = 1 \rightarrow \text{certain}$

highly likely

Ponder Impossible $P(I) = 0 \rightarrow \text{Impossible}$

$P(f) = 0.15, 0.1, 0.05$ } dependent on situation
highly unlikely.

$$P(\text{str}) = \#F/n = 3/6 = 1/2 = 0.5 \quad \text{event chance, moderate likely}$$

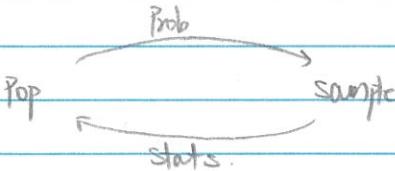
Complement: $P(\text{not the event})$. $P(\text{not } A)$, $P(A')$ or $P(A^c)$ or $P(\bar{A})$.

$$P(A) + P(A') = 1$$

$$P(A') = 1 - P(A)$$

Prob vs. Stat

- Stats: the sample is known
- Conclusion about population
- Prob: the population is known
- ask about sample, chance
- Stats reason from the sample toward the population
- Prob reason from the population toward the sample



Odd

- Special type of Prob
- Fav to UnFav
- $\text{Fav} = \text{Fav}' \text{ or } \text{Fav} / \text{Fav}'$
- Odd of tails on a coin: $T : T' \rightarrow 1 : 1$
- Odd of a 6 on a die: $F : F' \rightarrow 1 : 5$

4.1 (11, 14 ~ 17, 19).

(odd-tail) long-head

LOL #s (Law of Large numbers)

- Fallacy of the short run
- Law of Large numbers

Sample Space

• $S = \{\text{the set of all possible outcomes}\}$

• Corn Toss = $S = \{h, t\}$

• 2 corn = $S = \begin{Bmatrix} s & g \\ t & t \\ h & t \\ t & h \\ h & h \end{Bmatrix}$

round 1 Dr. k

round 2 coco cola.

round 3 Pepsi

① 病 ⑥ = ⑪ 自杀 → 非常不常见 & 非常常见 (大幅无危险)

② 死 ⑦ = ⑫ 车

③ = ⑧ gunshot (自) ⑬ 自杀

④ = ⑨ drug ⑩ 车

⑤ = ⑩ gun (他) ⑪ 车

$S = \left\{ \begin{array}{ccc} 1 & 2 & 3 \\ C & P & K \\ C & K & P \\ P & C & K \\ P & K & C \\ K & P & C \end{array} \right\}$ $P(\text{right}) = \frac{E}{n} = \frac{1}{6} = 16\frac{2}{3}\% = \text{unlikely}'$

Expected #: $E(X) = n \cdot P. = 25 \times \frac{1}{6} = 4.16$

09-05-2023

Lace of shoes

Hypothesis More Lace than none lace. G₂ G₃

Lace	None Lace
M = <u>1F</u> 2 4 3 7 ⑭	↓ M =
F = <u>1F</u> 1 2 12 16 ⑮	F = T ⑯

M 3 15	⑯	16	M 1	⑰
F 5 4 3 5	⑰	F	(5)	.

M ≠ 1 2 2 1 4	⑯	⑰	M 1	⑱
F ≠ 2 1 2 1 3	⑲	19	F = 1	⑳

(Good) Observation = none changing.

Saw People

Collect data

(Poor) Limited in Location (A Building)

Limit in People (Senior & Junior)(Undercover)(Teacher)

None sur. of population

No List

Limited in Time (rush)

Undercover (monday, Tue) Undercover (noon, Wed ..., Oct)

Population Lace wearing practice of ALL stds at OPHS early Sept 2023

n: 50+, gender (guess), Grade \leftarrow Sr Jrs
random selection.

not a survey.

Describe the struggle.



+ 3.3(7, 8, 11) Video

Chebychev's Theorem

$$1 - \frac{1}{k^2}, 1 - \frac{1}{k}$$

$$k \neq 1, k > 1$$

standard Deviation

$$2\text{sd} : 1 - \frac{1}{2^2} = \frac{3}{4} = 75\%$$

$$3\text{sd} : 1 - \frac{1}{3^2} = \frac{8}{9} = 88.9\%$$

$$4\text{sd} : 1 - \frac{1}{4^2} = \frac{15}{16} = 93.8\%$$

Textbook = PIII bluebox

1 sentence conclusion.

$$\text{Ex: } \bar{x} - 2s \text{ to } \bar{x} + 2s$$

$$29.1 - 4(1.7) \text{ to } 29.1 + 4(1.7)$$

$$22.3 \text{ to } 35.9$$

At least 93.8% of the students would fit into the group that volunteered from 22.3 to 35.9 hours each semester

+ 3.2(4, 16, 17) 17(c) (go with 88.9%)

P₉₉⁽¹⁾ / charn⁽²⁾ / Q₁, Q₂, Q₃⁽³⁾

(1) P₉₉, bit 99% of the people

(2)

(3) Q₂ = 50%, Median

Q₁ = 25%

Q₃ = 75%

18, 20, 21, 21, 21, 21, 22, 22, 22, 23, 23, 23, 23, 23, 23, 23, 23, 23, 23, 24, 24, 25, 25, 25, 25, 26, 27, 27, 30, 32, 35.

Outlier:

$$Q_1 = 22$$

$$Q_2 = 23$$

$$Q_3 = 25$$

$$Q_1 - 1.5 \times IQR = 17.5 \quad P_{25}$$

Med

$$P_{75}$$

$$Q_3 + 1.5 \times IQR = 29.5$$

$$P_{50}$$

30, 32, 35

IQR

$$Q_3 - Q_1 = 3$$

Ana =

center = 23 (Median)

shape = skewed right

spread = IQR = 3 "tight"

① 211 B \rightarrow Max.

3.3. 11

② Elon M. 180 B

a) low = CA high = Penn

③ Jeff B. 114 B

b) Penn

④ Larry E. 107 B

c) CA, Tex

⑤ Warren B. 106 B $\rightarrow Q_3 = 105$

d) (a) Texas

⑥ Bill G. 104 B

(b) Penn

⑦ Bloomberg 94.5 B

(c) CA

⑧ Hdu 93 B

⑨ Annbi 83.4 B

⑩ Baller 80.7 $\rightarrow Q_2(\text{Med}) = 80.6$.

⑪ 80.5

⑫ 79.2

⑬ 77.6

⑭ 76

⑮ 68 $\rightarrow Q_1 = 66.2$

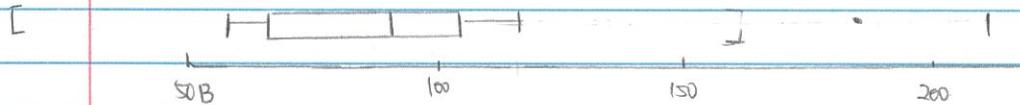
⑯ 67.4

⑰ 59

⑱ 59

⑲ 58.8

⑳ 57.6 \rightarrow Min.



\$ in Billion

Center = 80.6 (Med)

IQR

Spread = IQR, 38.8 = "Small"

CV

Shape: Skewed right

S

Outlier: $Q_1 - 1.5 \times \text{IQR} = 8$.

S^2

$Q_3 + 1.5 \times \text{IQR} = 163.2$

Range \rightarrow

180, 211.

cholychn

- + Don't assume people know a certain thing
- + No too long Question or long Survey
- + No leading (scandal) (corruption)
- + Double Negative
- + Context effect
- + Pre-test

- more about struggle
- limitation
- why (?)

09-27-2023

- face to face survey is bad (Response bias)

Survey

- Do you believe there are currently Terrorists

- Do you and your parent regularly discuss the news?

- "Regularly"

- How big is the news

- Assuming

- parents

- Yes or No

Please log the daily amount of time (min) spent discussing news with a trusted adult.

Mon state

national

global

Tue

...

2.3(127)

2.3 #7

min = 1.0 round $1.0 \rightarrow 1$

max = 29.8 $29.8 \rightarrow 30$

0 | 1 4
· 8 9 8 9 7 9 5

To fit your lung.

1 | 4 2 4 1 3 2

· 6 7 7 6 5 5 5 5 5

2

.

3 | 0

· $27 = 27 \text{ mg after}$

ctr: mode: 15 ~ 17

shape: skewed low.

sprad: ch3

out: 30

Survey 09-19-2023

- Ex:
- people are effect by others
 - + Survey
 - Word (Leading Suggest)
 - + Olympics
 - Peer influence (group setting)
 - Verbal (face, voice, body language)
 - Critics
 - 2016 vs. 2021 (^{younger} tend to give higher for recent)
- Not really. I didn't put much attention on sport.
- + written (not verbal)
 - still in group setting
 - + more individual
 - Word (phrases) (suggest)
 - + body more
 - Critics name
 - word
 - weak & Strong Opinion.

- 1 ② 3 4 5 Ordinal Data
- + written
 - still in group setting
 - + more individual
 - no option for "not watch"
 - + rank opinion
 - actually happened in 2021
 - + no city (no suggestion)
 - not center
 - + even # choices
 - equal spacing.

P4.

- + Right Now
- + number.

09-21-2023

	good	bad
AOL	+ balanced / non-suggestive question	AOL { - Picture, association
	+ equal spacing	- influence (word & picture)
	+ no slang	{ - too long.
OP Surf	+ clear options.	- Survey in group setting.
		- response bias
		{ - too many word.
		- "I believe" "should be made"
		leading
		- unequal space

Subway Survey

Good

Bad

- Voluntary Response Bias
- No enough option
- leading suggestive

Jamba juice

Good

Bad

- + short, less word.
- + Not leading
- + clear options
- Voluntary Response Bias
- Confusion option
- No Incentive
- Name, address, phone (X)

BBC

- Non-Random selective

+ Professional Organization.

- Influence leading

2.1 (6, 8, 15, 16, 22, 23)

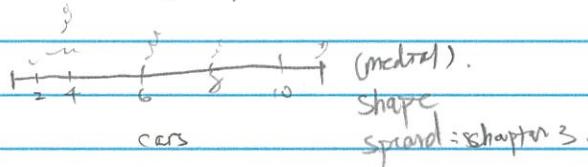
Shape of Histograms special bar graph.	Rectangular / Uniform	11111
	Bimodal	~
	Skewed Right	~ Look for the tail
	Skewed Left	~
	Symmetric	
	Symmetric / Normal	\ /

Dot Plot = need # line

similar to vertical graph

Quantitative data, mid size

not high spread.



of classes, usually 5-10,

$$w = \frac{\max - \min}{\# \text{ classes}} \text{ (round up)} (3.1 \sim 3.9 = 4) \quad w = \frac{44 - 14}{10} = \frac{30}{10} = 3.0 \text{ (Don't round)}$$

Begn with smallest value.

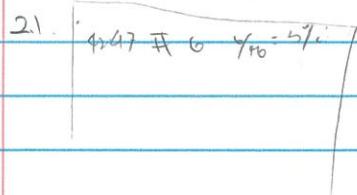
use class limits

class \rightarrow limits
14 ~ 16

lower limit \rightarrow 17

20

↓
41 ~ 49 < \leftarrow cap include more #



L

Stem & Leaf

① Max & Min.

② sorting data, $1|2 \leftarrow 2 \rightarrow 0|7$

③ Let the data flow

④ 2nd graph, put A in order

* Title, Key, Analysis.

Small &

1. max = 22

min = 2

2. tens ones.

3.	0	7	3	5	6	2	2	2	7	3
	1	0	0	4	0					
	2	2	0							

4. $0 | 2 2 3 3 5 6 7 | 7$
 $1 | 0 0 0 4$
 $2 | 0 2$

$2|0 = 20$ secs away

center = 7 (median).

shape = Skewed higher.

outlier = N/A

"line / stem"

① max = 25

0	2	2	3	3		mm = 3
5	6	7	7		② F	
1	0	0	0	4	7 6 5 3 5 7	0
.					5 5 3	5 6 5 5 5
2	0	2			8 7 5	1 0 0 7
.					5 0 0 5	2 5 5

P3

$1|4 = 14$ sec off

③

F | M

Ave - c

7 7 6 5 5 5 3 0 5 5 5 5 5 6 6

S

ctr = 7 8 5 1 0 0 7

S

Skewhigh 5 5 0 0 2 5 5

O

spread.

outlier = 25?

N/A

0 | 2

Fchmtrc

2|5 : 25 min

Matc

= 0|2|5 =

4.3 Study Guide

① Read P177~184

② When the outcomes are equally likely, how do we find $P(A)$?

$$P(A) = \frac{\text{Number of outcomes favorable to the event } A}{\text{Number of outcomes in the sample space.}}$$

③

④ a tree diagram

⑤

⑥ clerical factorial = $11! = 11 \times 10 \times 9 \dots \times 1$

$$0! = 1 = 1!$$

Permutation $P_{n,r} = \frac{n!}{(n-r)!}$
(order matter)
↑
order combinations.

Combination $C_{n,r} = \frac{n!}{r!(n-r)!}$
(order don't matter)

$n = \# \text{ of trials}$ $r = \# \text{ of successes}$

$C_{10,4}$ = the # of combination of 4 success out of 10 trials.

$$10C_4 = C_{10,4} = \frac{10!}{4!(10-4)!} = \frac{10!}{4!6!} = \frac{10 \cdot 9 \cdot 8 \cdot 7}{4! \cdot 1} = \frac{10 \cdot 9 \cdot 8 \cdot 7}{4 \cdot 3 \cdot 2 \cdot 1} = 210$$

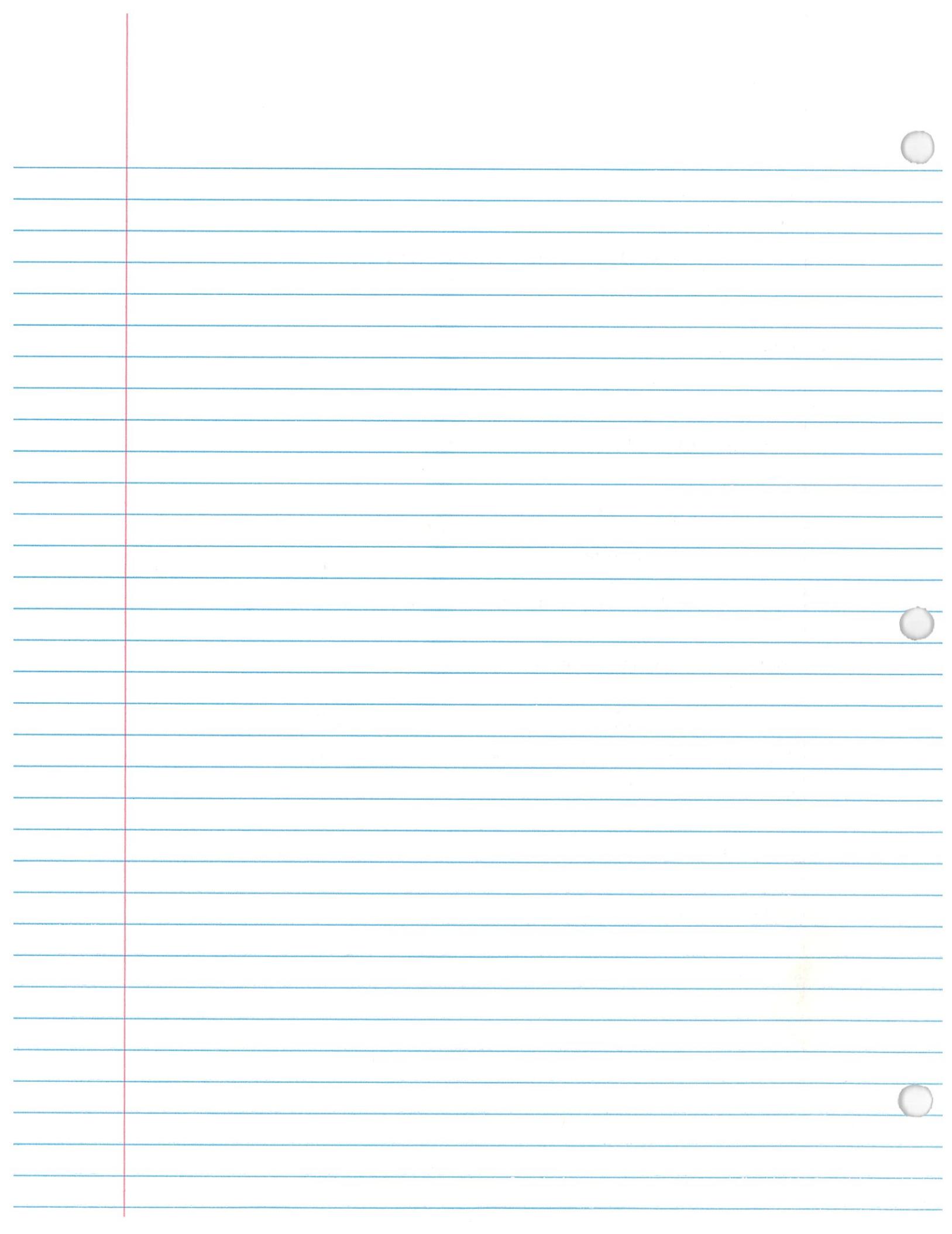
$P_{10,4}$ = the # of permutation of 4 success out of 10 trials

$$P_{10,4} = \frac{10!}{(10-4)!} = \frac{10 \cdot 9 \cdot 8 \cdot 7}{1} = 5040$$

$$P_{5,2} = 20 \quad P_{5,3} = 60 \quad P_{5,4} = 120 \quad P_{5,5} = 120$$

$$C_{5,5} = 1$$

4.3 (8, 9, 17 ~22)



5.1 Random Variables and Probability Distributions

Random Variables, X

Quantitative measurement, variable (X)

Ex: amount of snow fall

Non-Ex: nominal or ordinal

(5.1(1,3,10,12,14))

① continuous

② discrete

Discrete Random Variables

① countable, finite, (-3, -2, 0, 3, 7)

② No fractions, decimals, partial

③ # of voters in a election

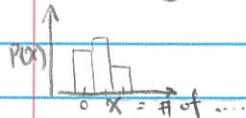
Continuous

① Quantitative, infinite countless.

② -2, -1, 0, 1, 2 and Fraction, decimals. Partial in between.

③ Ex: temp in room right now, ur height

Probability Distribution



$$\text{Expected value: } \mu = \sum x \cdot p(x)$$

Valid = add up to 1

$$\text{spread: } \sigma^2 = \text{Var}(X) = \sum (x-\mu)^2 \cdot p(x)$$

$$\sigma = \text{SD}(X) = \sqrt{\sum (x-\mu)^2 \cdot p(x)}$$

Ara:

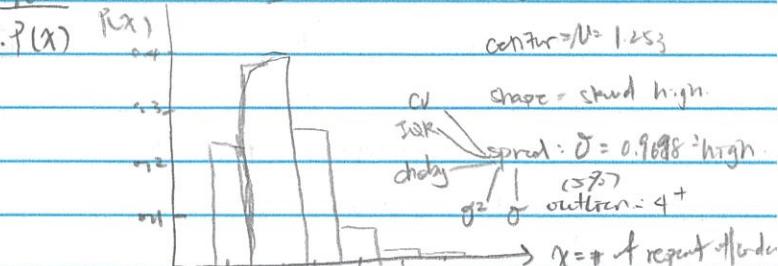
$$\text{contur} = \mu = 1.253$$

$$5.1(3) \text{ a) } 0.25 + 0.6 + 0.15 = 1 \text{ Valid}$$

$$\text{b) } 0.25 + 0.6 + 0.20 = 1.05 \text{ Non-Valid.}$$

$$14) \text{ a) } \bar{x} = \sum x \cdot p(x) \rightarrow x \cdot p(x)$$

$$= 1.253$$



$$\text{a) } P(X \geq 1) = P(X=1) + P(X=2) + \dots + P(X=5)$$

$$= 1 - P(X=0) = 1 - 0.237 = 0.763$$

$$\text{b) } P(X \geq 2) = P(X=2) + P(X=3) + \dots + P(X=5)$$

$$= 1 - (0.237 + 0.396) = 0.367$$

$$\div 1.253 = 0.7740 \text{ high spread.}$$

$$t \cdot L_1 = X \rightarrow \text{list}$$

$\downarrow \text{var}$

$$L_2 = P(X) \rightarrow \text{Frequenz}$$

5.2 (16, 18, 24)

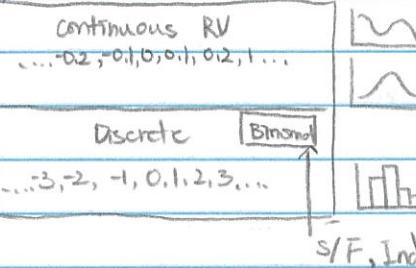
Binomial = Bernoulli (Swiss, 1600s)

↓
2 possible outcomes { Success
Failed.

- % →
- Probability of r successes out of n trials \rightarrow independent situation
 - p - probability of success $P^r = q$ $P + P^r = 1$ $P + q = 1$

of trial (asked purple), $n = 500$ } non-binomial.
of outcome possible = 500

Discrete Random Variable



S/F, Ind., $P = n = r/n$

Ex: ppt P_3

Trial = room call $Q = 0.2$

Ind = Yes $n = 72$

$S = 3^-$ min get $r = 63$

$F = 3^+$ min get

$P = 0.8$

Ex: Trial = yes or date Ind = Yes $S =$ say yes $F =$ say no $P = 71\% = 0.71$ $Q = 0.29$ $n = 20$ $r = 18+$

$$P(r) = \frac{n!}{r!(n-r)!} p^r q^{n-r} = C_{n,r} p^r q^{n-r}$$

$$n=6 \quad p=0.3 \quad q=0.7 \quad r=5$$

$$P(r) = (6,5 \times 0.3^5 \times 0.7^{6-5})$$

$$P(r) = 6 \times 0.00243 \times 0.7 = 0.0102$$

$$P(r=5) = 0.0102$$

[2nd] \rightarrow [vars] \rightarrow A: binompdf

Xvalue = r

Expected Number [of zombie]

$$n \cdot p$$

$$n=6 \quad p=0.7 \quad q=0.3 \quad r=4 \quad \text{Table A11}$$

$$P(r=4) = 0.324$$

$$P(r \geq 4) = P(4) + P(5) + P(6) = 0.324 + 0.303 + 0.118 = 0.745$$

Compound Event (2 or more events)

pair of dice = parabola (?)

$$P(A \text{ and } B) = P(A \cap B)$$

$$P(A) \times P(B)$$

$$P(5 \text{ and } 5) = P(5) \times P(5) = \frac{1}{6} \times \frac{1}{6} = \frac{1}{36} = 0.027 \text{ "highly unlikely"}$$

$$\begin{aligned} \text{place } & \xrightarrow{\text{②}} \text{No Replace } P(\text{Ace and Ace}) \\ & \stackrel{\text{①}}{=} P(\text{Ace}) \times P(\text{Ace}) = \frac{4}{52} \cdot \frac{4}{52} = \frac{1}{169} = 0.0059 \text{ "highly unlikely"} \\ & \stackrel{\text{②}}{=} P(A) \times P(A|A) = \frac{4}{52} \cdot \frac{3}{51} = \frac{1}{221} = 0.0045 \text{ "highly unlikely"} \end{aligned}$$

↓
Dependency

$$P(G \text{ and } B) = P(G) \times P(B|G) = \frac{1}{3} \times \frac{1}{2} = \frac{1}{6} = 16.7\% \text{ "unlikely"}$$

$$P(\text{all work}) = 0.977^6 = 0.8697$$

Yes ↗ 87% like
13% like
No ↗ 87% like
13% like

$P(A \text{ or } B)$: as long as someone got it done.  $P(A \cup B)$ either, add

$$= P(A) + P(B)$$

$$\begin{aligned} P(\text{King}) + P(\text{Ace}) &= \frac{4}{52} + \frac{4}{52} = \frac{8}{52} \leftarrow (-\text{Queen} \text{ and Grand dad}\right) \\ &= 0.1569 \text{ "pretty unlikely" } \end{aligned}$$

$$P(\text{King}) + P(\text{Heart}) = \frac{4}{52} + \left(\frac{13}{52} - \frac{1}{52} \right) = \frac{16}{52} = 0.3077$$

non-disjoint or non-mutually exclusive

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

4.1 4.2 (9, 13, 15, 18, 22)

blk br blu str gre gra pur
8 black, 7 brown, 6 blue, 4 dr., 4 green, 3 gray, 1 purple. = 33

$$P(\text{blk}, \text{blk}) = P(\text{blk}) \cdot P(\text{blk} | \text{blk}) = \frac{8}{33} \cdot \frac{7}{32} = \frac{56}{1056}$$

$$P(\text{br}, \text{br}) = P(\text{br}) \cdot P(\text{br} | \text{br}) = \frac{7}{33} \cdot \frac{6}{32} = \frac{42}{1056}$$

$$P(\text{blu}, \text{blu}) = P(\text{blu}) \cdot P(\text{blu} | \text{blu}) = \frac{6}{33} \cdot \frac{5}{32} = \frac{30}{1056}$$

$$= \frac{158}{1056} = 0.1496$$

$$P(\text{gre}) \cdot P(\text{gre} | \text{gre}) = \frac{4}{33} \cdot \frac{3}{32} = \frac{12}{1056}$$

pretty unlikely

$$P(\text{str}) \cdot P(\text{str} | \text{str}) = \frac{4}{33} \cdot \frac{3}{32} = \frac{12}{1056}$$

$$P(\text{gra}) \cdot P(\text{gra} | \text{gra}) = \frac{3}{33} \cdot \frac{2}{32} = \frac{6}{1056}$$

$$P(\text{pur}) \cdot P(\text{pur} | \text{pur}) = \frac{1}{33} \cdot \frac{0}{32} = 0 \frac{0}{1056}$$

odd

$$F = F'$$

$$P(1, 2, 3, 4, 5, 6, 7) = 0.6 \times 0.2^6 = 3.84 \times 10^{-5} = 0.0000384 = 0.00384 \rightarrow 99.99616.$$

$\frac{11}{13} = 0.8462$ = "highly likely" reality = "not enough likely" the sensitivity

$\frac{2}{13} = 0.1538$ = "highly unlikely" false-negative

$\frac{50}{70} = 0.714285$ = "moderate"

$\frac{20}{70} = 0.285714$ = "low likely"

$$P(\text{present} \wedge +) \frac{110}{200} = 55\%$$

$$P(\text{present} \wedge -) \frac{70}{200} = 10\%$$

$$P(A) = P(A|B) \leftarrow \text{independent}$$

a) $\frac{470}{1000} = P(N) = 47\% \quad P(M) = ?$

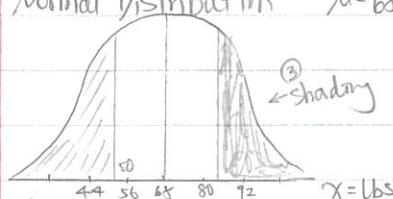
b) $P(N|M) = \frac{420}{500} = 84\% \quad P(N) \neq P(N|M) \text{ dependent}$

c) d) $P(N \wedge M) = \frac{120}{1000} = 42\%$

$$P(N \vee M) = P(N) + P(M) - P(N \wedge M) = \frac{470}{1000} + \frac{390}{1000} - \frac{120}{1000} = \frac{860}{1000} = 86\%$$

4.2 (9, 30) Pig, online. Edpuzzle

Normal Distribution $\mu = 68$ $\sigma = 12$



A) $X = 50$ $Z = \frac{50-68}{12} = -1.5$ $P(X < 50) = 0.0668$

← ② answer.

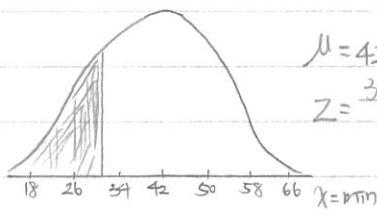
→ There is a 6.68% chance that a Pacific Yellowfin Tuna caught weight < 50 lbs.

B) $X = 85$ $Z = \frac{85-68}{12} = 1.42$ $P(X > 85) = 1 - 0.9222 = 0.0778$.

$Z = \text{STD}$ → There is a 7.78% chance that a Pacific Yellowfin Tuna caught weight > 85 lbs.
Notation $[1] \text{ndf} \rightarrow [2] \text{distr} \rightarrow [3] \text{normalcdf}$ ↑ words

c) $P(50 < X < 85) = 0.8549$.

→ There is a 85.49% chance that a Pacific Yellowfin Tuna caught weight between 50 & 85 lbs.

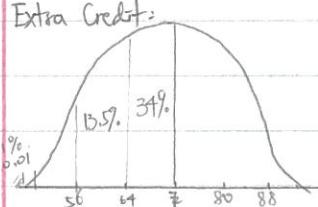


$\mu = 42$, $\sigma = 8$, $X = 30$

$Z = \frac{30-42}{8} = -1.5$ $P(X < 30) = 0.0668$

→ There is a 6.68% chance that response time of emergency will take less than 30 minutes.

Extra Credit:



$\mu = 72$ $\sigma = 8$ $[1] \text{distr} \rightarrow [3] \text{invNorm}$

1% unprotected. $53.39 \rightarrow \text{round down}$

53 hours.

6.3 (26, 28, 36) Extra = more video, 37.

Chapter 5 (9)

a) $n=16$ $P(r \geq 12) = 0.028 + 0.009 + 0.002 + 0 + 0 = 0.039$

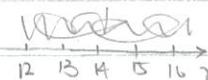
there will be

$P = 0.5$ $P(r)$

$q = 0.5$

$\frac{r}{n} = \frac{12}{16}$

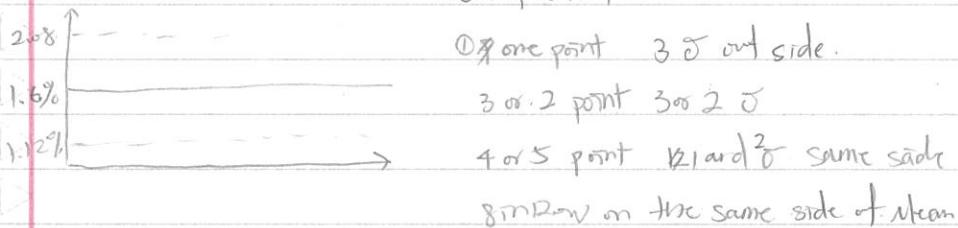
→ There is a 3.9% chance that 12 or more federal inmates are serving time for drug dealing.



c) $M = np = 16(0.5)$

Statistical Process Control.

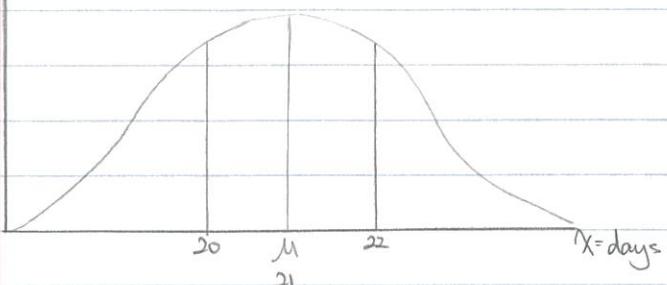
out of control.



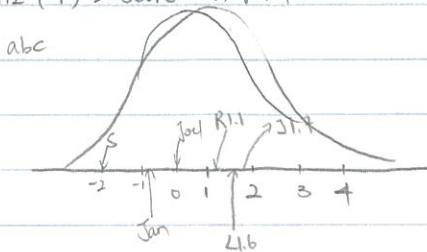
6.1 (1, 7, 8, 10)

$\mu = 20 \quad \sigma = 8$

$20 \sim 19 \quad \sigma \rightarrow \sigma - 2\mu \rightarrow 47.5\%$



6.2 (9) Z score = normal curve



d) Raw Score: $X = \sigma Z + \mu$

Juan: $1.7 = \frac{X-150}{20} \quad \text{Juan} = \frac{X-150}{20}$

Joel: $0 = \frac{X-150}{20} \quad 150 = X$

$34 = X - 150 \quad 150 = X$

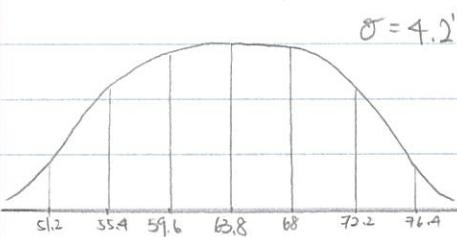
$X = 184$

Jan: $-0.8 = \frac{X-150}{20}$

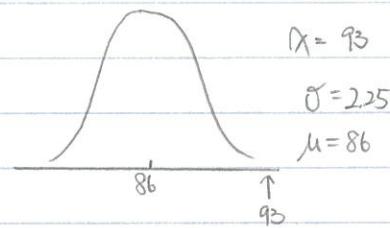
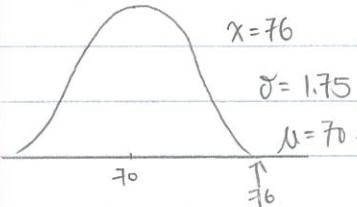
$-16 = X - 150$

$X = 134$

P299 figure 6-18

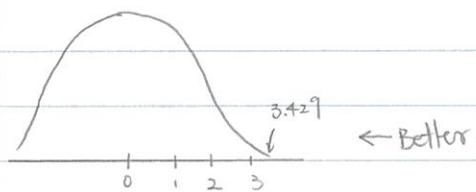


$Z = \frac{X - \mu}{\sigma}$ (不是越大越好, 看情况)



$Z = (76-70) \div 1.75 = 3.429$

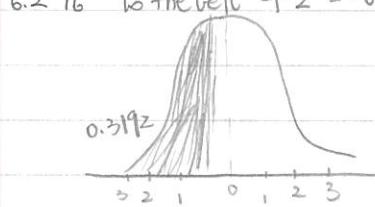
$Z = (93-86) \div 2.25 = 3.111$



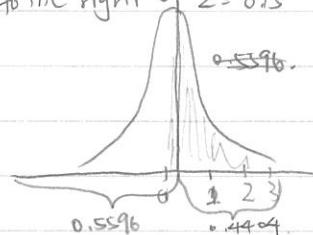
How many standard Deviation away
from μ .

percentiles - less or equal to a certain value (%) Ex: 75th percentiles - 95th are below = Top 5%.

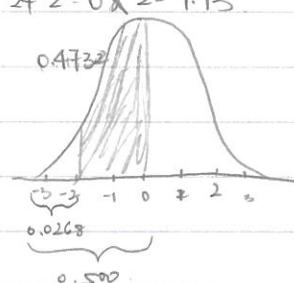
6.2 16 To the left of $Z = -0.47$.



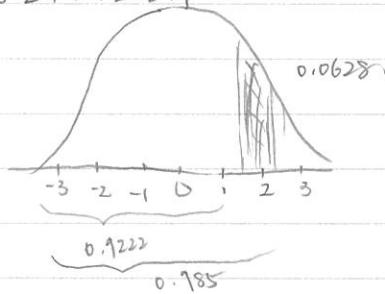
20 to the right of $Z = 0.15$.



24 $Z = 0.8$ $Z = -1.93$.



28 $Z = 1.42$, $Z = 2.17$

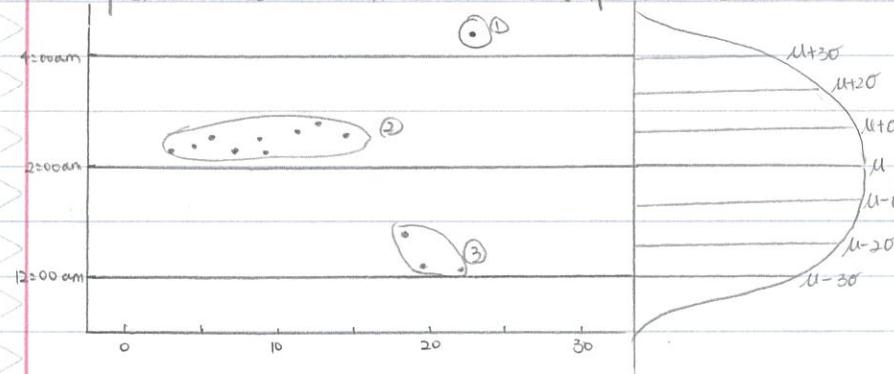


6.2 (4, 8, 9) (14, 40) ↪ (16, 20, 24, 28, 32).

Control Charts

Common cause variation = day-to-day factors

Special Cause Variation = sudden, unpredictable events

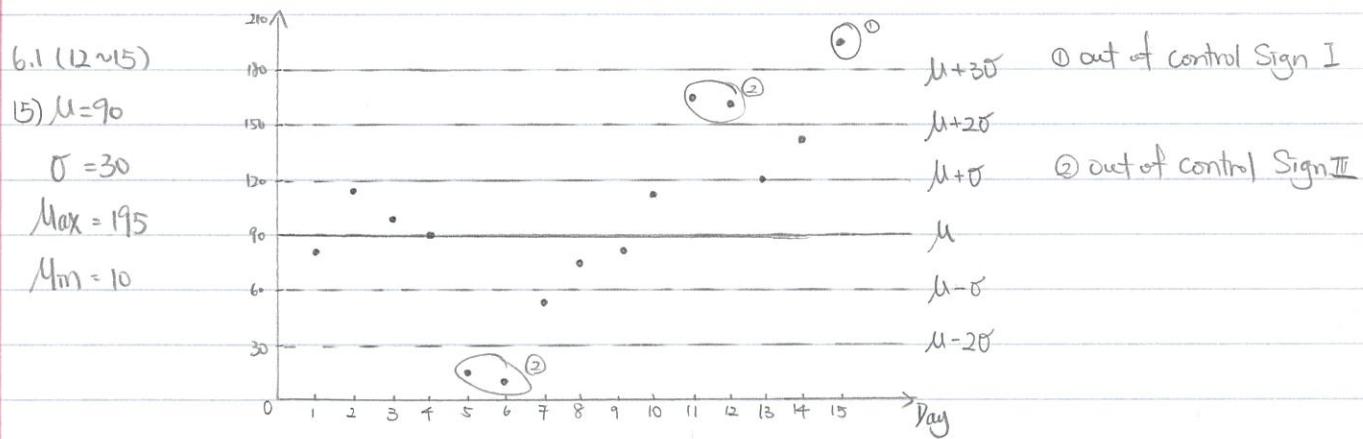


Out of Control:

① 1 point fall beyond 3σ

② 9 consecutive points on one side of μ .

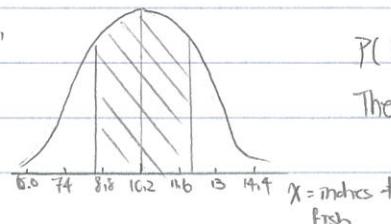
③ 2 + the 3 consecutive points lies beyond 2σ on the same side



Review

$$\mu = 10.2''$$

$$\sigma = 1.4''$$



$$P(8 < X < 12) = 0.8427$$

There exist a 84.27% chance that the size of the fish in the fishing pond is between 8" and 12".

6.4 Sampling Distribution

Population = All measurement of interest.

Sample = A subset of the measurements from the population.

random sample:

$$\mu, \sigma, \sigma, P, P, y = \alpha + bx$$

Population \rightarrow List

\downarrow ①

④ Inferential

Random sample

collect ②

Analysis ③

$$\bar{x}, s, s^2, r, r/n, y = \alpha + bx$$

Probability Theory - The Central Limit Theorem

Normal Probability Distribution

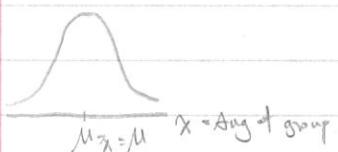
① The \bar{x} distribution is a normal distribution.

② The mean of \bar{x} distribution is μ .

③ The standard deviation

Orig X Distr

Normal



normalcdf

$$P(8 < \bar{x} < 12) = 99.77\%$$

lower: 8

higher

upper: 12

$$\mu = 10.2$$

$$\sigma = \sigma / \sqrt{n} = 1.4 / \sqrt{5}$$

$$\sigma_{\bar{x}} = \sigma / \sqrt{n} \leftarrow \text{"st crmr"}$$

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

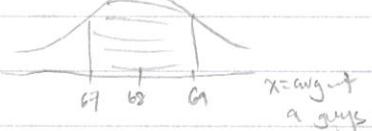
* n can be any # (Big or small)

The Central Limit

$$\mu = 68$$

$$\sigma = 3$$

$$P(67 < \bar{x} < 69) = 0.6827$$



$$\sigma_{\bar{x}} = \sigma / \sqrt{n}$$

$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

* n is BIG ≈ 30

$\bar{x} = \text{Avg of group}$

$$\mu = 90$$

$$P(38 < \bar{x} < 41) = 92.13\%$$

$$\sigma = 4.2$$

P of avg = Orig X Distr

$$n = 36 / 7 / 30$$

$$6.5(4, (6, 18))$$

$$0, 0, 0, 0, 6, 13$$

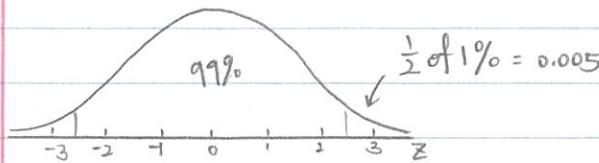
$$0, 0, 0, 0, 377$$

7.1 Estimation

Level of Confidence C.

Z_c

0%



-2.57 or -2.58

80%	1.28
90%	1.645
95%	1.96
99%	2.58

a) $E = Z_c \left(\frac{\sigma}{\sqrt{n}} \right)$

b) $\bar{x} - E < \mu < \bar{x} + E$

$\sigma = 180$, $\bar{x} = 15.60$, $n = 90$, c-level = 0.99

$E = (2.58) \left(\frac{180}{\sqrt{90}} \right) = 0.4895$

$15.6 - 0.4895 < \mu < 15.6 + 0.4895$

$15.11 < \mu < 16.09$

If we took 100 samples we expect to catch the population mean (μ) of just 99 occasions.

c) c-level = 80%, $n = 15$, $\sigma = 0.33$

If we took 100 sample we expect to catch the Pop.

$E = (1.28) \left(\frac{0.33}{\sqrt{15}} \right) = 0.1690$

mean (μ) of humming bird 80% time.

$0.33 - 0.1690 =$

$3.041 < \mu < 3.26$

$n = ? \quad n \uparrow \text{ c } \uparrow \quad n = \left(\frac{Z_c \sigma}{E} \right)^2$

d) $n = \left(\frac{1.28 \times 0.33}{0.08} \right)^2 = 27.88 \approx 28$ (always round up!) (Even -1, -2 ...)

7.1(15, 18, 19, 22).

7.2(15, 16, 18)

population	C-level	Zc	$n = \left(\frac{Zc\sigma}{E}\right)^2$
	80%	1.28	
	90%	1.645	If we took ...
	95%	1.96	
	99%	2.58	

$$\bar{x} - E < \mu < \bar{x} + E$$

+ formula = confidence intervals

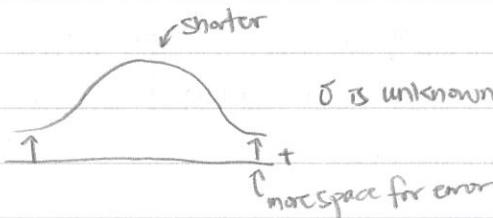
$$\bar{x} \pm t\left(\frac{\sigma}{\sqrt{n}}\right)$$

W.S. Gosset) - t-curve

chemist

Guinness Brewery

Ireland 1908



$$\bar{x} = 289, s = 1.8, n = 10, d.f. = n - 1.$$

$$289 \pm t\left(\frac{1.8}{\sqrt{10}}\right) \rightarrow 289 \pm 1.3$$

2.262

$$287.7 < \mu < 290.3$$

20 years $P = 0.80$

P/F $n = 20$ students

Ind.

Geometric Distribution

$$N = \frac{1}{P}$$

$$\sigma = \sqrt{\frac{1-p}{p}}$$

$$P = ?$$

$$n = ?$$

$$x = 1^{\text{st}} \text{ success}$$

continue ... -2, -1, 0, +1, 2 ... (& everything in between)	Rv

$$\rightarrow S/F, Ind$$

$$\rightarrow P, r/n$$

$$\mu = np$$

$$\sigma = \sqrt{np(1-p)}$$

first success $\rightarrow n = \# \text{ of trial on which we got our first success.}$

(geometric probability) \hookrightarrow 第几把为首次成功, 止于成功

distribution) n is not fixed number

$$P(n) = p(1-p)^{n-1}$$

$$\mu = \frac{1}{p}$$

$$\sigma = \sqrt{\frac{1-p}{p}}$$

$n = \# \text{ of binomial trial} \rightarrow \text{first success}$

$p = \text{probability of success on each trial}$

\hookrightarrow should stay the same.

8.26

X

$P(X)$

Risk Drives Detective = S

1

0.03

f.S 1st Failed, 2nd Success

$$0.97 \cdot 0.03 = 0.0291$$

F \rightarrow F \rightarrow S

$$(0.97)^2 \cdot 0.03 = 0.0282$$

D D W = F

2

0.0291

F \rightarrow F \rightarrow S

$$(0.97)^3 \cdot 0.03 = 0.0274$$

Ind

3

0.0274

$$(0.97)^4 \cdot 0.03 = 0.0266$$

$$P = 0.03$$

4

0.0266

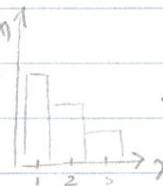
$$q = 0.97$$

5

0.0266

$$P(X=n) = q^{n-1} p$$

$P(X)$



\hookrightarrow always step down.

8.41

$$S = \left\{ \begin{array}{l} HHH, TTT \\ HHT, TTH \\ HTT, FHF \\ FTH, THF \end{array} \right\} \quad P = 0.75 \quad q = 0.25$$

$$P(X=3) = 0.25^{3-1} \cdot 0.75 = 0.0469$$

5.4(10, 11)

8.26, 8.41

5 trials = shot (basket) Binomial

Success = in $n=5$

Failed = miss $r=4$

$$p = 0.7$$

$$q = 0.3$$

Independent

4th success. Geometric

trial = catch the ball

Success = catch Independent

Failed = miss

$$P(X=n) = q^{n-1} \cdot p$$

$$\sigma = \sqrt{q/p}$$

$$P(X=4) = 0.3^4 \cdot 0.7 = 0.189$$

$$p=0.7 \quad q=0.3$$

Independent

$$P = 0.25 \quad P(X=n) = q^{n-1} \cdot p$$

$$q = 0.75 \quad P(X=17) = 0.75^{17-1} \cdot 0.25$$

Success = win $= 0.0025$

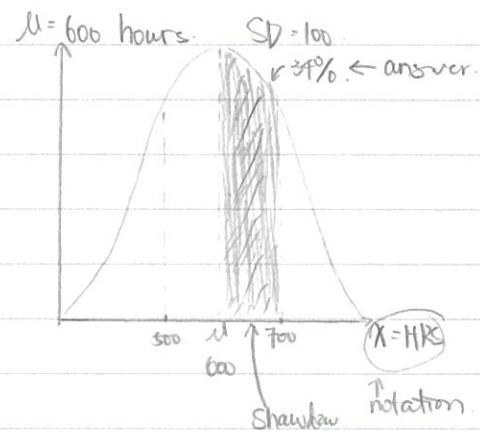
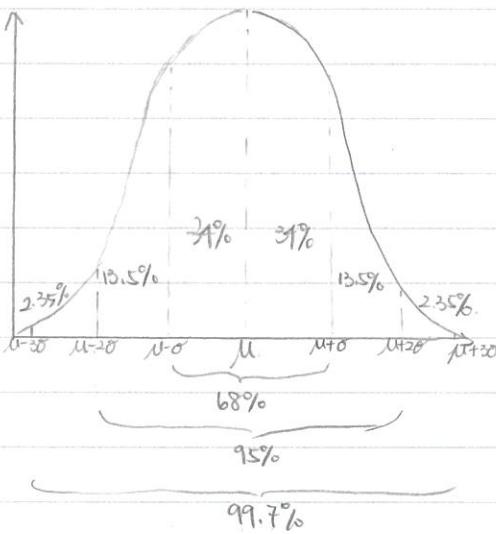
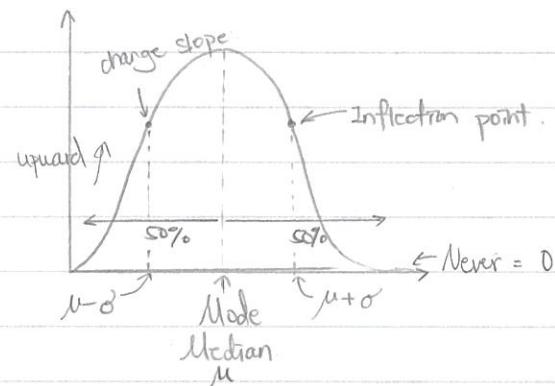
Failed = lose calculator

$n = 17$ th 2nd \rightarrow vars \rightarrow distr \rightarrow F: geom pdf

stop = 17th get (win). $P = p \quad X = \text{stop}$

ch 6 Normal Distribution

	Continuous RV
	-2, -1, 0, 1, 2 (and everything)
	normal (bell)
(Geo)	Discrete (BT) ← Same



① High bias, ~~low~~ variability. **high variability**

② Low bias, Low variability. **Good job**

③ Low bias, High variability

④ High bias, low variability.

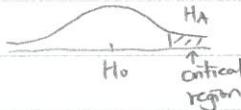
Hypothesis = a assumption or belief about parameter. "accept" or "reject"

Null Hypothesis: H_0 . The champ. = "No change" = "No Difference" Tradition.

Alternate Hypothesis: H_1 or H_a . the challenger, better way. accepted if Null reject.

$H_0: \mu = 3 \text{ hrs}$

$H_A: \mu > 3 \text{ hrs}$



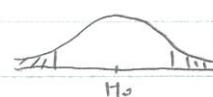
$H_0: \mu = 3 \text{ hrs}$

$H_A: \mu < 3 \text{ hrs}$



$H_0: \mu = 3 \text{ hrs}$

$H_A: \mu \neq 3 \text{ hrs}$



Accept Null

Reject Null

Null hypothesis →
is true

Correct
Conclusion

Type I Error
rejected a true
null hypothesis

α = Level of Significance
 $0.01, 0.05, 0.10$
 $1 - \alpha = c$

The true states
of nature



Null hypothesis
is False

Type II Error
accept a false
null hypothesis

$\beta =$

Correct
Conclusion
 $\text{Power} = 1 - \beta$

4 Ingredients to Stats Test 8.1(16,17)

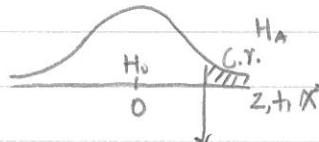
① H_0

→ stay in population

$$\alpha = 0.05$$

② H_1 or H_A $>, <, \neq$

$$\text{level} = 0.95$$



$$p\text{-value} = 0.2805 \quad \boxed{\alpha = 0.05}$$

"wern"

③ C.V. critical value

weak evident vs. null.

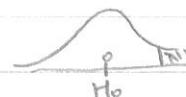
$$④ \bar{X} = \dots \rightarrow Z$$

$$p\text{-value} = 0.0280 \quad \boxed{\alpha = 0.05}$$

"Stern"

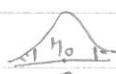
$$17) \text{a)} \quad H_0: \mu = 16.4$$

$$\text{b)} \quad H_1: \mu > 16.4$$



strong evident vs. null

$$d: H_1: \mu \neq 16.4$$



If the p-value is low, the H_0 should go.

8.1(21,24) 8.2(11,12) (Popp)

P457

$$\text{Known, } \sigma \text{ unknown, } df = n-1, \bar{X} \rightarrow t = \frac{\bar{X} - \mu}{S/\sqrt{n}}$$

+ -table $\rightarrow df \rightarrow$ find $t \rightarrow$ two or one-tail \rightarrow Range $0.02 < p\text{-value} < 0.05$

8.2(18,19,20)

$$18) \mu = 14, \bar{X} = 15.1, S = 2.51, \alpha = 0.01, n = 10, df = 9, \text{ higher (1-tail).}$$

$$t_c = \pm 2.821. \quad t = (15.1 - 14) / [(2.51) / \sqrt{10}] = 1.39.$$

$H_0: \mu = 14$ Inefficent SSes

$H_A: \mu > 14 \quad 0.1 > p\text{-value} > 0.075 \quad \boxed{\alpha = 0.01} \quad \text{"wern"}$

$$20) \mu = 77, \bar{X} = 71.4, S = 20.65, n = 20, df = 19, \alpha = 0.05, \text{ less (1-tail).}$$

$$t_c = \pm 1.729 \quad t = (71.4 - 77) / (20.65 / \sqrt{20}) = -1.21$$

$H_0: \mu = 77$ Inefficent SSes

$H_A: \mu < 77 \quad 0.125 > p\text{-v} > 0.100 \quad \boxed{\alpha = 0.05} \quad \text{"wern"}$

8.3 (9, 10, 12)

$$Z = \frac{\hat{P} - P}{\sqrt{P(1-P)/n}} = \hat{P}$$

Z_c = critical value

$P = 0.67$ $\hat{P} \rightarrow Z = (0.5526 - 0.67) / \sqrt{(0.67)(0.33)/38}$

$n = 38$ $= -1.5391$

$r = 21$ $\neq = -1.54$

$\alpha = 0.05$

"less"

$\hat{P} = 0.5526$

8.3 (9)

purple / white

8 Review (S27) with TI-84

Monday Test

Hypothesis Test (Dependent)

• 2 groups

• Before / After

• Matching link (natural match)

Advantages:

reduce the danger of extra factor

reduce variation

\bar{d} mean difference between the paired data

$= \bar{x}$ (sample mean) (difference \neq).

S_d sample standard deviation

T-Test

$t = 1.07$

$P = 0.1553$

$H_0: \mu_d = 0$ The average difference of μ_d is 0

foot drop metric ≈ 0

$H_A: \mu_d > 0$

$\alpha = 0.1$ $n = 11$ $df = 10$

$$\bar{d} \rightarrow t = \frac{\bar{d} - \mu_d}{S_d / \sqrt{n}}$$

$$= 1.07$$

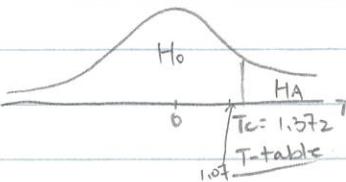
$H_0 H_A$ fail to reject the null

$\exists x$ less than or more feet different
than μ_d is > 0

i. $\mu_d = 0$

p-value = 0.1553 $| \geq | \alpha = 0.1$

"Wcm"



Ex: 2 tests for each patients (dependent)

8.4(9,12,20) Vid 28

$$H_0: \mu_d = 0 \quad H_A: \mu_d > 0$$

$$T = 6.6661 \quad P = 9 \times 10^{-4}$$

① Test $\mu_1 - \mu_2$ when σ_1 & σ_2 is known.

$$Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

$$Z_c \rightarrow \alpha$$

8.5 (15,17,18). Extra: Perils highlight

② Test $\mu_1 - \mu_2$ when σ_1 & σ_2 is unknown.

$$\sigma \rightarrow S$$

$$Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

$$t_c \rightarrow \text{table}$$

8.5 (19,25,26)

15. Test \Rightarrow ③

17. Test \Rightarrow ③

Z-Test of Difference of 2 Independent Mean

$H_0: \mu_{\text{child}} = \mu_{\text{adult}}$. The average REM sleep time of children is same as adult.

$$H_A: \mu_{\text{child}} > \mu_{\text{adult}} \quad \alpha = 0.01 \quad Z_c = 2.58$$

$$n_1 = 10 \quad n_2 = 10$$

$$\bar{X}_1 = 2.8 \quad \bar{X}_2 = 2.1$$

$$\sigma_1 = 0.5 \quad \sigma_2 = 0.7$$

26, L3, L4

T-Test of \bar{Y} of 2 Ind. Mean

$$\alpha = 0.05$$

$$H_0: \bar{M}_1 = \bar{M}_2$$

$$H_A: \bar{M}_1 < \bar{M}_2$$

$$t = -1.1263 \quad P = 0.1402$$

19) L5, L6

T-Test of \bar{D} of 2 Ind. Mean

$$\alpha = 0.01$$

$$H_0: \bar{M}_{\text{NE}} = \bar{M}_{\text{RM}}$$

$$H_A: \bar{M}_{\text{NE}} < \bar{M}_{\text{RM}}$$

$$t = -0.9524 \quad P = 0.1761$$



Quiz

- ① Dependent
- ② Independent
- ③ Dependent
- ④ Dependent
- ⑤ Independent
- ⑥ Dependent Ind.

have have not.

$$n_1 = 792 \quad n_2 = 490 \quad \rightarrow 20 \text{ months}$$

death rate:

$$\hat{P}_1 = 14.2\% \quad \hat{P}_2 = 19.8\% \quad \boxed{b = 2 - \text{Prop Z Test}}$$

$$Y_1 = 112 \quad Y_2 = 97$$

$$P = 0.0077 \quad \boxed{\alpha = 0.01}$$

"sean"

chi-Square

#9. $\alpha=0.05$ 3×2

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

O	E	O-E	$(O-E)^2$	$(O-E)^2/E$
62	49.02	12.98	168.48	3.44
68	74.22	-6.22	38.69	0.5212
56	62.76	-6.76	45.69	0.7280
45	57.98	-12.98	168.48	2.91
94	87.78	6.22	38.69	0.4408
81	74.24	6.76	45.69	0.6154

$$\chi^2 = \sum = 8.64$$

Inference Template

Name: _____

Problem Number: 9.3 Ps85 Ex 8

Name of Test/Interval:

Null and Alternative Hypotheses:

(in words and symbols) $H_0 : \rho = 0$

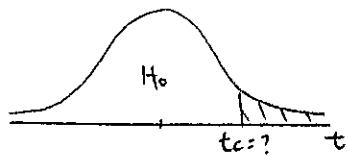
$$\beta = 0$$

$$H_A : \rho \neq 0$$

$$\beta \neq 0$$

Check of Conditions:

Math Box: (standard deviation, test statistic, p-value, margin of error, sketch, etc...)



$$\begin{matrix} t \\ b \end{matrix} \rightarrow t = 7.56$$

Decision and conclusion:

• ~~H_0~~ $\textcircled{H_A}$ $\alpha = 0.01$

• $\exists X$ uses x (age of wolves) and y (weight) has positive correlation and positive slope.

• $p\text{-value} = 0.0003 \blacksquare \alpha = 0.01$

"Seam"

③ Test of Difference of Proportions. $\hat{p}_1 - \hat{p}_2$

$$\text{large values } \hat{p}_1 - \hat{p}_2 = \frac{r_1}{n_1} - \frac{r_2}{n_2}$$

$\downarrow \rightarrow$ 数据, 统计出来的

can be unknown.

$$\mu = \hat{p}_1 - \hat{p}_2 \quad \sigma = \sqrt{\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}}$$

$$\hat{p} = \frac{r_1 + r_2}{n_1 + n_2}$$

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\hat{p} \hat{q}}{n_1} + \frac{\hat{p} \hat{q}}{n_2}}}$$

stat \rightarrow TESTS \rightarrow 6:2-Prop Z Test $\quad X_1 = r_1, \quad X_2 = r_2 \quad 8.5(29, 33 \sim 35)$.

7.4 confidence intervals for $\mu_1 - \mu_2$ (6.8.12 \times or \checkmark) & $\hat{p}_1 - \hat{p}_2$. $7.4(18 \sim 19)$

① $\mu_1 - \mu_2, \sigma_1, \sigma_2$ known

② $\mu_1 - \mu_2, \sigma_1, \sigma_2$ unknown

$$E = z_c \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

$$E \approx t_c \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$(\bar{x}_1 - \bar{x}_2) - E < \mu_1 - \mu_2 < (\bar{x}_1 - \bar{x}_2) + E$$

same

d.f. = $n_1 - 1 \rightarrow$ go with the
smaller one
 $= n_2 - 1$

\bar{x}_1, \bar{x}_2 = sample mean

same

n_1, n_2 = sample size

7.4 stat \rightarrow TESTS \rightarrow 9 or 10 or B

③ $\hat{p}_1 - \hat{p}_2$

$$E = z_c \hat{\sigma} = z_c \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}}$$

$$(\hat{p}_1 - \hat{p}_2) - E \leq \hat{p}_1 - \hat{p}_2 \leq (\hat{p}_1 - \hat{p}_2) + E \rightarrow \boxed{\text{unit!}}$$

notation $\rightarrow \mu_1 - \mu_2$

for ① & ②

for ③

$$+ \rightarrow + \Rightarrow \mu_1 - \mu_2 > 0$$

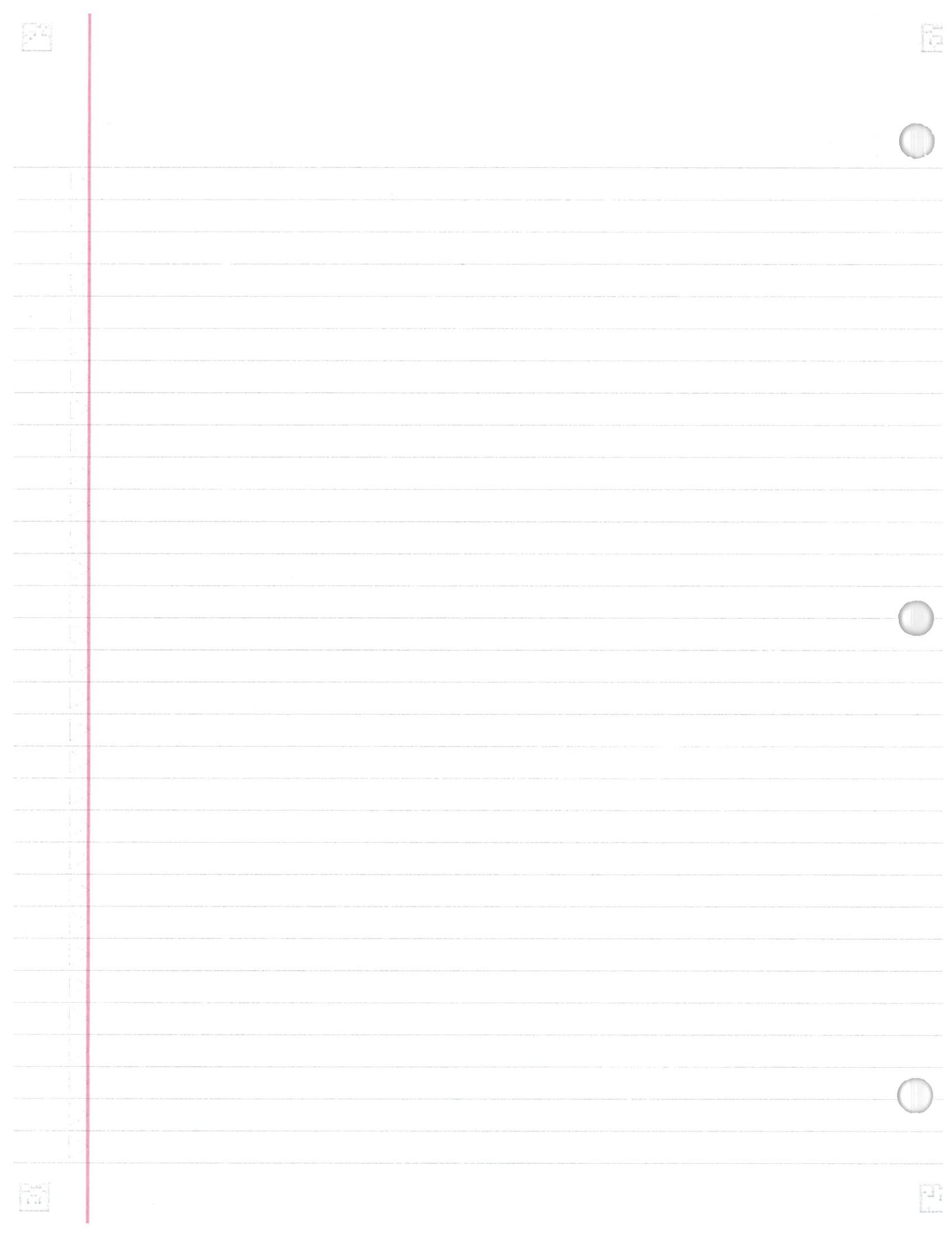
$$\Rightarrow \mu_1 > \mu_2$$

$$TV_1 > TV_2$$

\therefore Group 1 who ... brain wave is greater than Group 2.

$$- \rightarrow - \Rightarrow \mu_1 < \mu_2 \quad TV_1 < TV_2$$

$$- \rightarrow + \Rightarrow \mu_1 \approx \mu_2 \quad TV_1 \approx TV_2$$

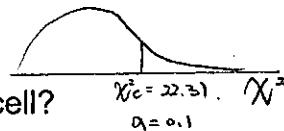


10.1 Chi-Square Study Guide

1. Read pp. 624 through 630
2. Draw a 4 by 6 contingency table

		1	2	3	4	5	6
*							

3. Put a * in cell #7
4. Chi-squared distributions test the independence of 2 factors always white #
5. T/F The graph of χ^2 is symmetrical Irony of factors O-E observe - Expect
6. T/F As the d.f. increase, the χ^2 distribution becomes more skewed right
7. Where's the mode/high point on a χ^2 distribution? $n-2$.
8. How does one calculate the critical value for χ^2 ?
 $\alpha = ?$ df = ? $\rightarrow \chi^2$ table



9. Which is correct for finding the expected frequency of a cell?

$$\frac{\text{row total} * \text{column total}}{\text{sample total}} \quad \text{OR} \quad \frac{\text{row total} * \text{column total}}{\text{sample total}}$$

same

10. Find E for cell #9 table 10-2

$$E = (100)(60) / (300) = 20$$

11. Symbolize observed frequencies

12. χ^2 measures O-E / Independent
13. Use the χ^2 formula to justify the authors' claim in guided exercise 3 that $\chi^2 = 13.31$. Show your work.

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

14. Is that "it"? What else do we do?

15. How does one calculate the d.f.?

$$df = (\text{rows}-1)(\text{columns}-1)$$

16. Find the d.f. for your contingency table in #2 above.

$$df = (4-1)(6-1) = 15.$$

17. Do 10.1 (9)



10.2 Chi Square Goodness of Fit

$$E = \% \times n$$

$$\text{Sample size} \quad \chi^2 = \sum \frac{(O-E)^2}{E}$$

O = observed

$$H_0: \chi^2 = 0$$

$$H_A: \chi^2 > 0$$

df. = k - 1 → # of categories in the distribution.

P690 Table 10-8

10.2 (6, 10, 13) + PPUSD

$$13) E = 1215 \times 10\% = 121.5 \quad \alpha = 0.01$$

$$121.5 \times 0.03 = 36.45 \quad \chi^2 = 13.6829$$

$$121.5 \times 0.38 = 461.7 \quad p\text{-value} = 0.0178$$

$$121.5 \times 0.41 = 498.15 \quad \chi^2_c = 15.09$$

$$121.5 \times 0.06 = 72.9 \quad \text{df.} = 6-1=5$$

$$121.5 \times 0.02 = 24.3$$

Sample stat

s

s.d.

population

σ

s^2

Variance

σ^2

$$\text{Theorem 10.1} \quad \chi^2_{\text{score}} = \frac{(n-1)s^2}{\sigma^2}$$

$$H_0: \sigma^2 = k \quad \begin{matrix} \nearrow \text{number} \\ \searrow \end{matrix}$$

$$\chi^2_c = \rightarrow \text{Table 8 df.}$$

$$H_A: \sigma^2 \geq k \rightarrow \begin{matrix} \nearrow \text{most} \\ \searrow \text{some} \end{matrix}$$

10.3 (6, 8, 9) 4: c.c.

Scatterplot

$$9.2 \text{ 15) } \sum x = 112.8 \quad \sum y = 32.4 \quad \sum x^2 = 2167.14 \quad \sum y^2 = 90.14 \quad \sum xy = 665.3 \quad r \approx 0.764$$

$$x = 24 \quad y = ?$$

$$y = a + bx$$

$$a = -17.204$$

$$b = 1.202$$

ANA = +/ - Association

STAT \rightarrow CALC \rightarrow 18 \rightarrow ①

$$r^2 = 0.5836$$

$$r = 0.7640$$

- As ...

$$-1 \leq r \leq 1$$

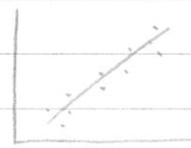
$$r = -1$$



$$r = +1$$



$$r = 0.81$$



outlier (

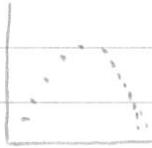
- r = correlation.

r^2 = coefficient of determination

$$r = 0$$



$$r = 0$$



$r = 0.7640$ Moderately strong

Linear correlation

$r^2 = 0.5836$ 58.36% of variation in y (violent crime)

is explained by variation in x (lung no school)
the Least Square Regression Line

mode 2

CALCULATOR \rightarrow r & r^2 \rightarrow STAT DIAGNOSTICS

$$a = y\text{-intercept}$$

$$b = \text{slope}$$

trend line:

$$a = -17.204$$

$$b = 1.202$$

From ① $\rightarrow y = ? \rightarrow$ Vars $\rightarrow 5 = ? \rightarrow$ EQ $\rightarrow 1 = ? \rightarrow$ zoom $\rightarrow 9 = ?$

point:

2nd \rightarrow trace \rightarrow calc $\rightarrow 1 = ? \rightarrow x = ?$



$$\hat{y} = a + bx$$

LSRL

$$\hat{y} = -17.20 + 1.20x$$

$$\hat{y} = -17.204 + 1.202(24)$$

$$\hat{y} = 11.64$$

ρ = "rho" population correlation coefficient

β = "Beta" population slope

9.3 (7, 9, 10) Test (only b & f) (ex.g.)

Thurs (9 & 10)

9 in class.

confident Interval of $\beta \rightarrow$ Data in List \rightarrow stat \rightarrow TEST \rightarrow C =

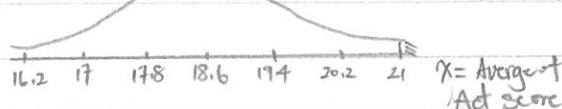
① 1998 26	⑪ 2010 <u>14</u> ₂	⑫ 2021 3	median ≈ 15
② 1986 38	⑫ 2017 7	⑬ 2016 28	mean: $> 15 \approx 18,19,20$
③ 2015 9	⑬ 2002 22	⑭ 2000 24	spread: 1279 High spread
④ 1997 27	⑭ 2016 <u>8</u>	⑮ 2014 10	
⑤ 2012 12	⑮ 1992 32	⑯ 2012 <u>12</u> ₁	$12 \quad 150/10 = 15$
⑥ 1996 28	⑯ 2006 <u>18</u>		14
⑦ 2019 5	⑰ 2016 <u>8</u>		12
⑧ 1981 35	⑱ 2019 <u>5</u>		18
⑨ 2014 10	⑲ 2012 <u>12</u>		12
⑩ 2000 24	⑳ 2006 <u>14</u>		28
			24
			8
			10
			12

ACT

$$\mu = 18,6 \quad \sigma = 5,9 \quad n = 50 \quad P(\bar{X} > 21)$$

There exist a 0,2% chance that 50 student

$$\sigma = 5,9 / \sqrt{50} = 0,8344 \quad \text{score mean is higher than 21}$$



$$\mu = \sum x \cdot p(x)$$

$$\$1,000,000 / \text{day} \times 365 \rightarrow 365,000,000 \Rightarrow 3,650,000,000$$

11 by hand
↓
9.2 (10~12, 15)

Nov. 9th (part) 9.1 ~ 9.2

$93\% \Rightarrow 4SD$.

$$\bar{x} = 20.35$$

$$20.35 + (4 \times 9.79) = 59.51$$

$$20.35 - (4 \times 9.79) = -18.81$$

At least 93.8% of the data is captured between -18.81 to 59.51 cm/gm/sec.

HT WS
62" 59"

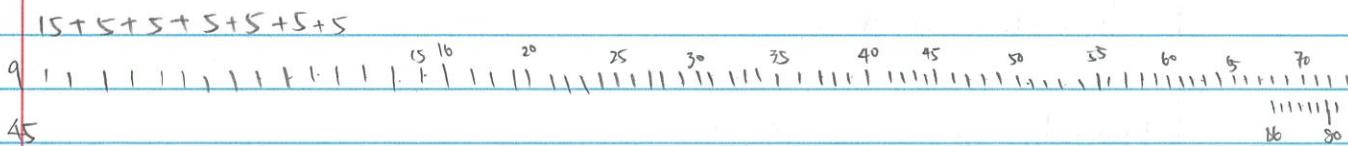
Analysis Ex + Association / + linear association

- Trend (with word) = the greater the wing spans , the higher the height .

- outlier (can point) / outlier = (60, 80)

Influential Score = the point is following the trend, but "out" of the data.

- Correlation = Not Now.



$$b = \frac{n\sum xy - (\bar{x}\bar{y})(\bar{x}\bar{y})}{n\bar{x}^2 - (\bar{x}\bar{x})^2} = \frac{7(1015) - (329)(115)}{7(18,263) - (108,241)} = -0.4964$$

$$\Sigma X = 329 \quad \bar{X} = 47 \quad \Sigma X^2 = 18,26$$

11. *Leucosia* *leucostoma* *leucostoma* *leucostoma* *leucostoma*

$$\Sigma X = 329 \quad X = 41 \quad \Sigma X^2 = 18,263$$

$$\bar{x}_4 = 115 \quad \bar{q} = 16.43$$

$$\Sigma xy = 4015$$

$$e = \bar{h} -$$

$$a = y - bX = 16.43 - (-0.4964)(47) = 31.76$$

$$\hat{y} = 39.76 - 0.4964x$$

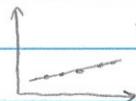
$$f) \quad g = 39.76 - 0.4964(25) = 27.35\%.$$

Formula way *

$9, N(13, 15, 18)$ easier way

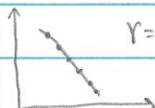
Correlation (Karl Pearson)

$$(r) -1 \leq r \leq 1 \quad r \neq b$$

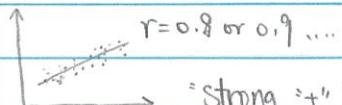


$$r=1 \quad b \rightarrow \text{smaller}$$

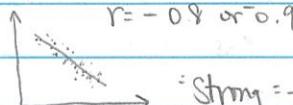
Perfect Linear Correlation
"PLC"



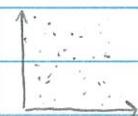
Perfect Linear negative Correlation.
"PLnc"



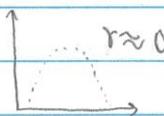
"Strong "+"LC"



"Strong =- "LC"



$$r \approx 0$$



$$r \approx 0$$

$$r = \frac{n\sum xy - (\sum x)(\sum y)}{\sqrt{n\sum x^2 - (\sum x)^2} \sqrt{n\sum y^2 - (\sum y)^2}}$$

$$\text{Determination} = r^2 \quad 0 \leq r^2 \leq 1$$

$$(-0.969)^2 = 0.9490$$

$r^2 = 0.9490 = 94.90\%$ of the variation in y (# of muggings) is explained by the LSRL and the variation in x (# of VPDs).

$$\text{b) } \sum x = 63$$

$$(\sum x)^2 = 3969$$

$$\sum y = 650$$

$$(\sum y)^2 = 422,500$$

$$\sum x^2 = 1089$$

$$\sum y^2 = 95,350$$

$$\sum xy = 9930$$

$$r = \frac{5(9930) - (63)(650)}{\sqrt{5(1089) - 3969} \sqrt{5(95,350) - 422,500}} = \frac{8700}{(38.42)(232.92)} = 0.9722$$

Strong Positive Linear Correlation

$r^2 = 0.9453 = 94.53\%$ of the variation in y (weight of the pony) is explained by the least square regression line and the variation in x (age of the pony)

$$\mu = ? \quad \sigma = ?$$

② have x find area% ③ have area% find x .

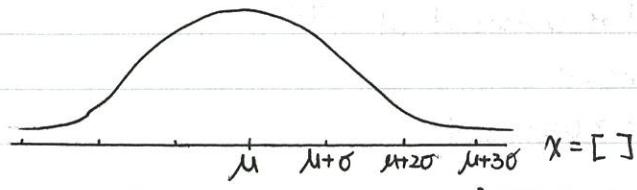
6.3 ② $P(?) < X < ?) = (?)\%$ ① calc: 2nd \rightarrow distr \rightarrow [2] normal cdf. $\exists x$ (?)% chance that
③ find x calc: 2nd \rightarrow distr \rightarrow [3] mvNorm. [] is [$</>/?</?$]

6.5 A random sample

$$\mu = ? \quad \sigma_x = \sigma / \sqrt{n}$$

$$P(?) < \bar{X} < ?) = (?)\%$$

① $\exists x$ (?)% chance that a sample of



68% - 34%

95% - 13.5%

99.7% - 2.35%

$$Z = \frac{x - \mu}{\sigma}$$

$$Z = \frac{x - \mu}{\sigma / \sqrt{n}}$$

8.7.2

7.1 necessary sample size $n = \left(\frac{Z_c \sigma}{E}\right)^2$ $\bar{X} - E < \mu < \bar{X} + E$ (unit!)

$$E = 2 \text{ or } t \times \left(\frac{\sigma \text{ or } S}{\sqrt{n}}\right)$$

calc: stat \rightarrow TEST \rightarrow [7] ZInt / [8] TInt.

7.3 necessary sample size $n = pq \left(\frac{Z_c}{E}\right)^2$ $\hat{p} - E < p < \hat{p} + E$

$$E = 2x \left(\frac{\hat{p}q}{n}\right)$$

calc: stat \rightarrow TEST \rightarrow [A] 1-Prop ZInt.

If we took X sample we expect to catch population mean μ (or) population % p of
[] y times. (for \hat{p} , $n = \dots$)

7.4 Z-T Interval of Difference of 2 Mean / Proportion (Ind)

$$\# < p_1 - p_2 < \# \quad \text{calc: stat} \rightarrow \text{TEST} \rightarrow [9] \boxed{10} \boxed{11}$$

80% 1.28 95% 1.96

90% 1.645 99% 2.58.

$$\mu_1 - \mu_2$$

$\rightarrow + \Rightarrow \mu_1 \approx \mu_2 \quad p_1 \approx p_2 \quad []$ is equal to / less than / greater than [].

$\rightarrow - \Rightarrow \mu_1 < \mu_2 \quad p_1 < p_2$

$\rightarrow + \Rightarrow \mu_1 > \mu_2 \quad p_1 > p_2$

8.1~8.3 Z/T-Test of 1-mean / p (Ind)

8.4. T-Test of Dep Mean

calc: TEST \rightarrow [1] [2] [5] $H_0: \mu =$

calc: Ln(differences) \rightarrow TEST \rightarrow [2]

8.5 Z/T-TEST of Difference of 2 Ind. M/p.

calc: TEST \rightarrow [3] [4] [6] $\hat{p} = r/n$

9.189.2 $\hat{y} = a + bx$ and r, r^2 calc: stat \rightarrow CALC \rightarrow [8]

mode \rightarrow STAT DIAGNOSTICS.

Ana: +/- Association

$-r = x$ (Strong...) +/- (Linear Correlation)

Influential / Outliers. $-r^2 = x$ % of variance in $y()$ is explained by LSR and variance in $\hat{y}()$.

9.3 T-Test of Population correlation ρ and β . $r \rightarrow t = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}}$ calc = # in $\text{list} \rightarrow \text{stat} \rightarrow \text{TEST} \rightarrow [F=]$. $H_0: \rho = 0$ x & y have no correlation. β Interval: $\Rightarrow [G=]$. $\beta = 0$ population slope of LRL is flat.

10.1 Chi-Square Test of Ind. \square

calc: $[2nd] \rightarrow \text{matrix} \rightarrow \text{Edit}$.

$\text{stat} \rightarrow \text{TEST} \rightarrow [C]$

$$E = \frac{\text{rowtotal} \times \text{column}}{\text{sample total}}$$

$$\text{df.} = (\text{row}-1)(\text{column}-1)$$

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

10.2 Chi-Square Test of Goodness of fit. \equiv

df. = # of categories - 1

calc: $\text{stat} \rightarrow \text{edit} \rightarrow O=L_1, E=L_2$

$\text{TEST} \rightarrow [D]$

$$E = \% \times n$$

$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

10.3 Chi-Square Test of Variance

$$H_0: \sigma^2 = \#$$

$$\chi^2_{\text{scr}} = \frac{(n-1)s^2}{\sigma^2}$$

calc: $[2nd] \rightarrow \text{distr} \rightarrow [8=]$ (p -value).